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Clearly fill out this cover page and the top portion of the provided bubble sheet  
with the necessary information.

Do not open the exam until told to do so.

When prompted, clearly print the information required at the top of  
each page of this exam booklet.

For multi-select questions, you receive partial credit for each correct answer  
choice as long as you select none of the incorrect answer choices.

You can remove the equation sheet(s). Otherwise, keep the exam booklet  
intact. You will have 60 minutes to complete the examination.

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4) An object's position is described by  $x(t) = (-8 - 4t + 3t^2)m$ . Which of the following statements is TRUE?

- A. At  $t = 0$ , the object is at the origin.
- B. The object slows down for all values of  $t$ .
- C. It stops instantaneously at  $t = 8.0\text{ s}$
- D. It stops instantaneously at  $t = 0.67\text{ s}$ .
- E. The object never stops because it is already moving at the time  $t = 0$ .

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5) Which of the following will remain in the air for the LEAST amount of time (neglecting air resistance)?

- A. A marble launched straight up from the ground at  $9.8\text{ m/s}$
- B. A marble launched from the ground with a speed of  $9.8\text{ m/s}$  at an angle of  $30^\circ$  from the horizontal
- C. A marble that is dropped straight down from a  $50\text{ m}$  high building.
- D. A marble that is launched horizontally from a  $50\text{ m}$  high building

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6) The only forces acting on a  $2.0\text{-kg}$  ball are shown below. What is the magnitude of the acceleration of the ball?

$$\vec{F}_1 = (2\hat{i} - 8\hat{j})\text{N}$$

$$\vec{F}_2 = (5\hat{i} - 3\hat{j})\text{N}$$

- A.  $5.2\text{ m/s}^2$
- B.  $6.5\text{ m/s}^2$
- C.  $3.0\text{ m/s}^2$
- D.  $3.2\text{ m/s}^2$
- E.  $4.3\text{ m/s}^2$

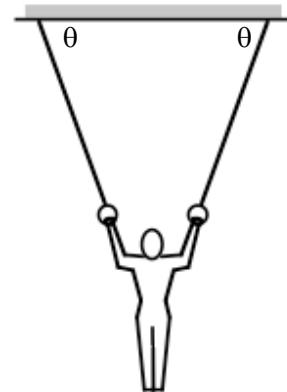
**NOTE: Questions 7, 8 and 9 can have more than one correct answer. For each question, select all answers that are correct.**

- 7) A rotating disk is slowing down during a time interval of one second. Which of the following combinations of the initial angular velocity,  $\omega_i$ , final angular velocity,  $\omega_f$ , and angular acceleration,  $\alpha$ , could describe this motion? **Select all that are correct.**

- |                                   |                                |                              |
|-----------------------------------|--------------------------------|------------------------------|
| A. $\omega_i = -3 \text{ s}^{-1}$ | $\omega_f = -5 \text{ s}^{-1}$ | $\alpha = -2 \text{ s}^{-2}$ |
| B. $\omega_i = -5 \text{ s}^{-1}$ | $\omega_f = -3 \text{ s}^{-1}$ | $\alpha = +2 \text{ s}^{-2}$ |
| C. $\omega_i = +3 \text{ s}^{-1}$ | $\omega_f = +5 \text{ s}^{-1}$ | $\alpha = -2 \text{ s}^{-2}$ |
| D. $\omega_i = -3 \text{ s}^{-1}$ | $\omega_f = -5 \text{ s}^{-1}$ | $\alpha = +2 \text{ s}^{-2}$ |
| E. $\omega_i = +5 \text{ s}^{-1}$ | $\omega_f = +3 \text{ s}^{-1}$ | $\alpha = -2 \text{ s}^{-2}$ |

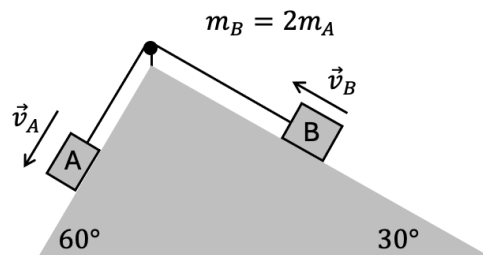
- 8) A gymnast weighing 500 N is suspended by two ropes from the ceiling as shown. The gymnast is at rest. The lengths and angle,  $\theta$ , indicated are the same for the two ropes. **Select all that are correct.**

- A. The magnitude of the tension in the rope on the left is greater than 250 N.
- B. The magnitude of the tension in the rope on the left is less than 250 N.
- C. The magnitude of the tension in the rope on the left is equal to 250 N.
- D. The magnitude of the tension in the two ropes are the same.
- E. The magnitude of the tension in the two ropes are different.



- 9) Two blocks, A and B, where  $m_B = 2m_A$ , are connected by a massless, inextensible string that passes over a frictionless pulley. The blocks are sliding on frictionless surfaces. At the instant shown, block A is moving down its ramp, while B is moving up. **Select all that are correct.**

- A. At this instant, Block A is slowing down.
- B. At this instant, Block A is speeding up.
- C. At this instant, Block A is moving with constant speed.
- D. At this instant, the blocks' accelerations have the same magnitude.
- E. At this instant, the blocks' velocities have the same magnitude.





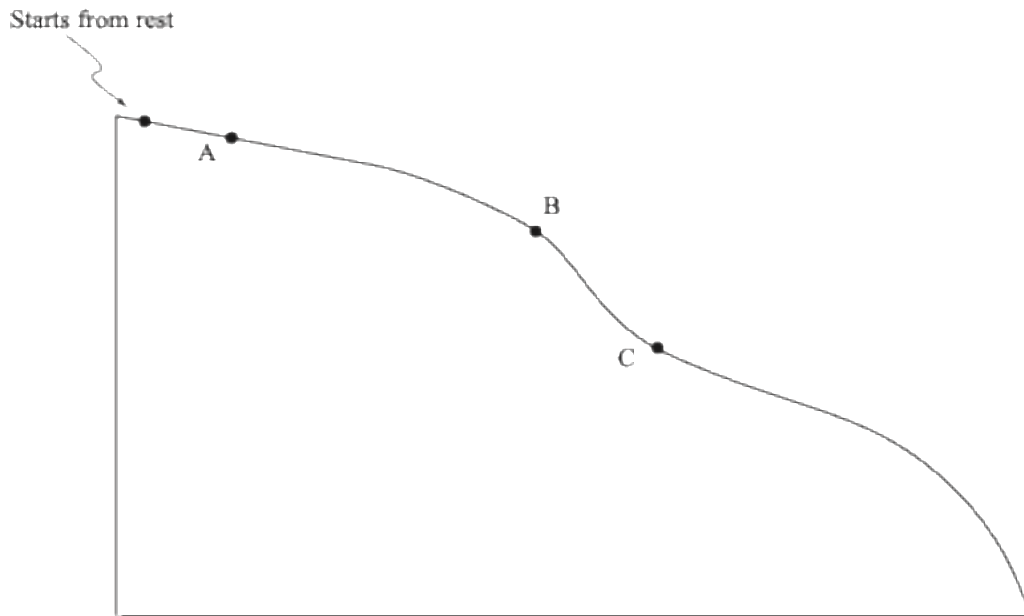






**IV. Tutorial Free Response (15 pts – 3 questions)**

A sled on snow moves along a hill as shown. At point A, the hill is a straight line. Assume there is negligible friction between the sled and the snow and the sled speeds up throughout the motion.



17) [6 pts] At each of points A, B, and C, draw vectors to show the velocity and acceleration of the sled.

**For point B:**

18) [4 pts] Explain your reasoning for how you decided to draw the **velocity** vector at point B.

19) [5 pts] Explain your reasoning for how you decided to draw the **acceleration** vector at point B.

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## Constants

Free-fall acceleration	$g = 9.80 \text{ m/s}^2$
Gravitational constant	$G = 6.67 \times 10^{-11} \text{ N m}^2/\text{kg}^2$

## Mathematics

Vector components  $\vec{A} = \vec{A}_x + \vec{A}_y = A_x \hat{i} + A_y \hat{j}$

Vector magnitude  $A = \sqrt{A_x^2 + A_y^2}$

$\theta$  ccw from  $x$ -axis  $A_x = A \cos \theta$   
 $A_y = A \sin \theta$   
 $\theta = \tan^{-1}(A_y/A_x)$

Adding vectors  $\vec{C} = \vec{A} + \vec{B}$   $C_x = A_x + B_x$   
 $C_y = A_y + B_y$

Dot product  $\vec{A} \cdot \vec{B} = AB \cos \alpha$   
 $\vec{A} \cdot \vec{B} = A_x B_x + A_y B_y$

Cross product  $|\vec{A} \times \vec{B}| = AB \sin \alpha$   
 $\vec{A} \times \vec{B} = -\vec{B} \times \vec{A}$

Standard deviation  $s = \sqrt{\frac{\sum_{i=1}^n (x_i - x_{\text{ave}})^2}{n-1}}$

## Linear motion

Average velocity  $\vec{v}_{\text{ave}} \equiv \frac{\Delta \vec{r}}{\Delta t} = \frac{\vec{r}_f - \vec{r}_i}{t_f - t_i}$

Instantaneous velocity  $\vec{v} = \frac{d\vec{r}}{dt}$

Instantaneous acceleration  $\vec{a} = \frac{d\vec{v}}{dt}$

Constant acceleration (in “s” direction)

$$v_{fs} = v_{is} + a_s \Delta t$$
$$s_f = s_i + v_{is} \Delta t + \frac{1}{2} a_s (\Delta t)^2$$
$$v_{fs}^2 = v_{is}^2 + 2 a_s \Delta s$$

Motion on inclined plane  $a_s = \pm g \sin \theta$

Relative motion  $\vec{v}_{CB} = \vec{v}_{CA} + \vec{v}_{AB}$

## Circular motion

Angular position  $\theta = \frac{s}{r}$

Angular velocity  $\omega = \frac{d\theta}{dt}$

Angular acceleration  $\alpha = \frac{d\omega}{dt}$

Tangential velocity  $v_t = \omega r$

Centripetal acceleration  $a_r = \frac{v_t^2}{r} = \omega^2 r$

Tangential acceleration  $a_t = \alpha r$

Period  $T = \frac{2\pi r}{v} = \frac{2\pi}{\omega}$

Const. angular acceleration  $\omega_f = \omega_i + \alpha \Delta t$

$$\theta_f = \theta_i + \omega_i \Delta t + \frac{1}{2} \alpha (\Delta t)^2$$

$$\omega_f^2 = \omega_i^2 + 2 \alpha \Delta \theta$$

## Force and motion

Newton’s 2<sup>nd</sup> law  $\vec{a} = \frac{\vec{F}_{\text{net}}}{m}$

Gravity  $F_G = mg$

$$F_G = \frac{GMm}{R^2}$$

Maximum static friction  $f_{s \text{ max}} = \mu_s n$

Kinetic friction  $f_k = \mu_k n$

Reynolds number  $Re = \frac{\rho v L}{\eta}$

Drag (high  $Re$ )  $F_{\text{drag}} = \frac{1}{2} C_d \rho A v^2$

Drag (low  $Re$ )  $F_{\text{drag}} = 6\pi \eta r v$

Newton’s 3<sup>rd</sup> law  $\vec{F}_{A \text{ on } B} = -\vec{F}_{B \text{ on } A}$

Circular motion  $(F_{\text{net}})_r = \frac{mv_t^2}{r} = m\omega^2 r$

$$(F_{\text{net}})_t = ma_t$$

## Work and energy

Kinetic energy  $K = \frac{1}{2} m v^2$

Work by a constant force  $W = \vec{F} \cdot \Delta \vec{r}$

Hooke’s law  $(F_{\text{sp}})_s = -k \Delta s$

Work done by a spring  $W = -\frac{1}{2} k [(\Delta s_f)^2 - (\Delta s_i)^2]$

Dissipative force  $\Delta E_{\text{th}} = f_k \Delta s$

Potential energy  $\Delta U = -W_{\text{int}}$

Grav. potential energy  $U_G = mgy$

Elastic potential energy  $U_{\text{sp}} = \frac{1}{2} k (\Delta s)^2$

Mechanical energy  $\Delta E_{\text{mech}} = \Delta K + \Delta U$

System energy  $\Delta E_{\text{sys}} = \Delta E_{\text{mech}} + \Delta E_{\text{th}}$

$$\Delta E_{\text{sys}} = W_{\text{ext}}$$

Power  $P = \frac{dE_{\text{sys}}}{dt}$

$$P = \vec{F} \cdot \vec{v}$$

Force and potential energy  $F_s = -\frac{dU}{ds}$

### Impulse and linear momentum

Momentum  $\vec{p} = m\vec{v}$

Impulse  $\vec{J} \equiv \int_{t_i}^{t_f} \vec{F}(t) dt$

Momentum principle  $\Delta\vec{p} = \vec{J}$

Isolated system  $\vec{P}_f = \vec{P}_i$

Force  $\vec{F} = \frac{d\vec{p}}{dt}$

Elastic collision with  $(v_{ix})_2 = 0$

$$(v_{fx})_1 = \frac{m_1 - m_2}{m_1 + m_2} (v_{ix})_1$$

$$(v_{fx})_2 = \frac{2m_1}{m_1 + m_2} (v_{ix})_1$$

### Rotation

Center of mass  $x_{\text{cm}} = \frac{1}{M} \sum_i m_i x_i$

Moment of inertia  $I = \sum_i m_i r_i^2$

Rod (center)  $\frac{1}{12}ML^2$

Rod (end)  $\frac{1}{3}ML^2$

Disk  $\frac{1}{2}MR^2$

Hoop  $MR^2$

Solid sphere  $\frac{2}{5}MR^2$

Hollow sphere  $\frac{2}{3}MR^2$

Parallel-axis theorem  $I = I_{\text{cm}} + Md^2$

Rotational kinetic energy  $K_{\text{rot}} = \frac{1}{2}I\omega^2$

Torque  $\tau \equiv rF \sin \phi = rF_{\perp} = Fd$   
 $\vec{\tau} \equiv \vec{r} \times \vec{F}$

Gravitational torque  $\tau_{\text{grav}} = -Mgx_{\text{cm}}$

Newton's second law for rotation

$$\alpha = \frac{\tau_{\text{net}}}{I}$$

Critical angle  $\theta_c = \tan^{-1} \left( \frac{t}{2h} \right)$

### Rolling

$$v_{\text{cm}} = R\omega$$

$$K_{\text{rolling}} = \frac{1}{2}I_{\text{cm}}\omega^2 + \frac{1}{2}Mv_{\text{cm}}^2$$

Angular momentum  $\vec{L} \equiv \vec{r} \times \vec{p}$

Angular momentum of a particle

$$L_z = mrv_t = mr^2\omega$$

Angular momentum of a rigid body

$$\frac{d\vec{L}}{dt} = \vec{\tau}_{\text{net}}$$

$$\vec{L} = I\vec{\omega}$$

### Theory of gravity

Law of gravity  $F_{1 \text{ on } 2} = F_{2 \text{ on } 1} = \frac{Gm_1m_2}{r^2}$

Free-fall acceleration  $g = \frac{GM}{r^2}$

Potential energy  $U_G = -\frac{Gm_1m_2}{r}$

Satellite speed  $v = \sqrt{\frac{GM}{r}}$

Kepler's third law  $T^2 = \left( \frac{4\pi^2}{GM} \right) r^3$

Escape speed  $v_{\text{escape}} = \sqrt{\frac{2GM}{R}}$

Geosynchronous orbit  $r_{\text{geo}} = \left( \frac{GM}{4\pi^2} T^2 \right)^{1/3}$